

at Hvar (October 1-7, 2017)

Spin Seebeck and Spin Peltier Effects

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References:

- * S. Maekawa(ed.) “Concepts in Spin Electronics” (Oxford University Press, 2006),
- * S. Maekawa et al. (eds.) “Spin Current” (Oxford University Press, 2017),

OXFORD SCIENCE PUBLICATIONS

Spin Current

Second Edition

Edited by

Sadamichi Maekawa,
Sergio O. Valenzuela,
Eiji Saitoh,
and Takashi Kimura



Second Edition:
Published in September 2017

* “[Spin Current](#)”(First Edition) : (Oxford University Press, 2012),

Outline

Spin Seebeck Effect and Spin Peltier Effect:

i) Spin Seebeck Effect:

Review Article,

**[K.Uchida, H.Adachi, T.Kikkawa, A.Kirihara, M.Ishida, S.Yorozu,
S.Maekawa and E.Saitoh, Proc. IEEE 104, 1946 (2016)].**

ii) Spin Peltier Effect:

Y. Ohnuma , M.Matsuo and S.Maekawa: to be published in Phys. Rev. B (2017).

Co-Workers:

Theory:

Y. Ohnuma (ASRC, JAEA),

H. Adachi (ASRC, JAEA → Okayama U.),

M. Matsuo (ASRC, JAEA).

Experiment:

E. Saitoh (Tohoku U.) and members in his group,

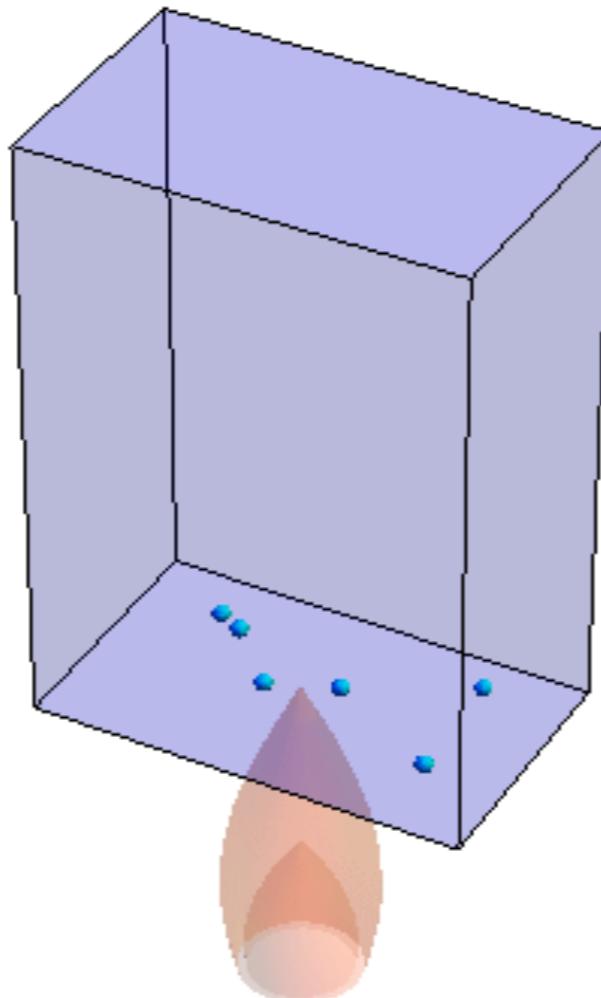
K. Uchida (Tohoku U. → NIMS, Tsukuba) ,

Heat vs. Electricity

	To get Electricity	To get Heat
Charge	Seebeck effect	Peltier effect
Spin	Spin Seebeck effect Uchida 2008	Spin Peltier effect Flipse 2014 Daimon 2016

Seebeck effect, spin Seebeck effect

Boiling of water



**Boiling of electrons
(Seebeck effect)**

**Boiling of spin current
(spin Seebeck effect)**

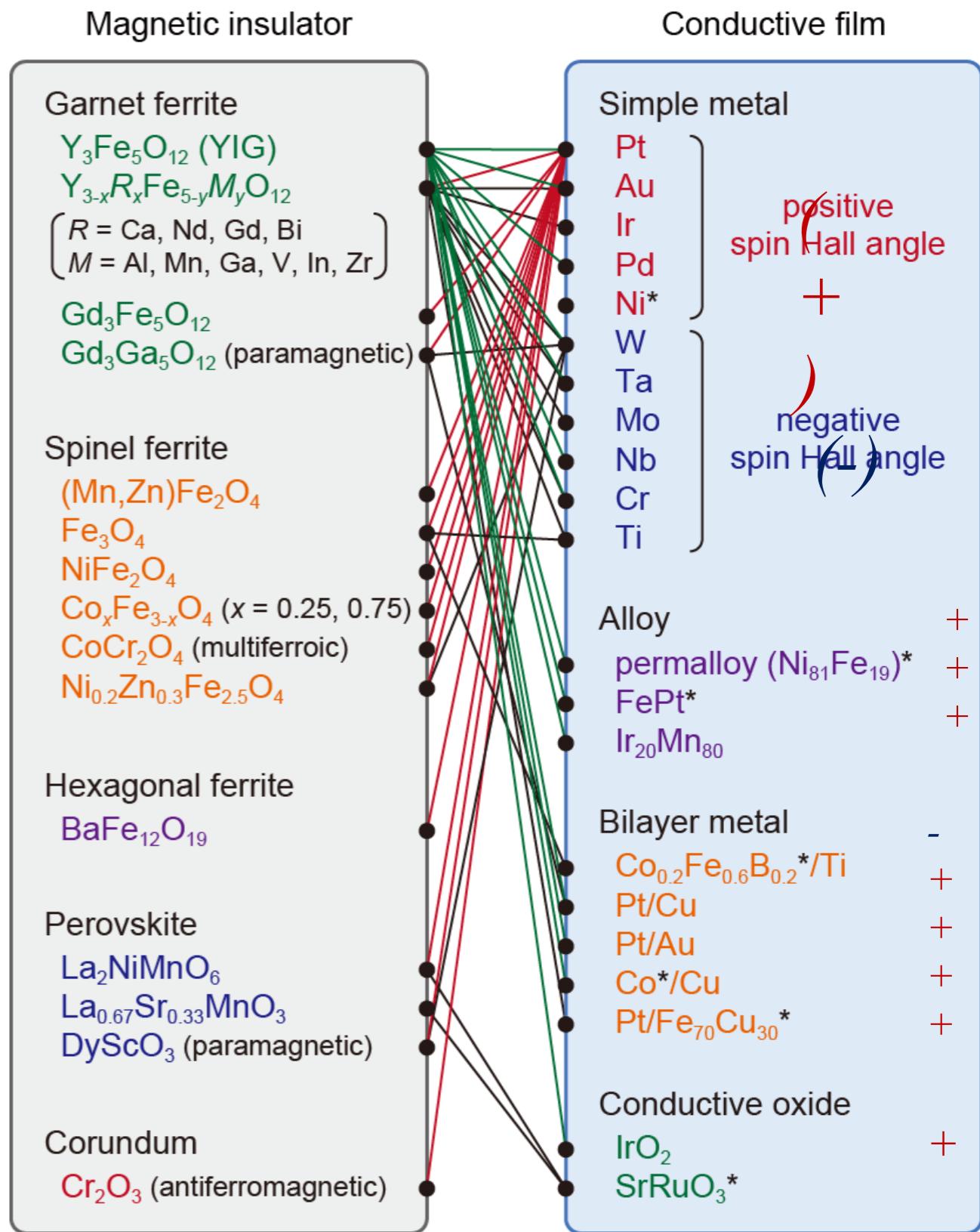
Combination of magnetic insulators and conductive films used for measuring SSE

SSE is a universal phenomenon in magnetic materials

Model system:

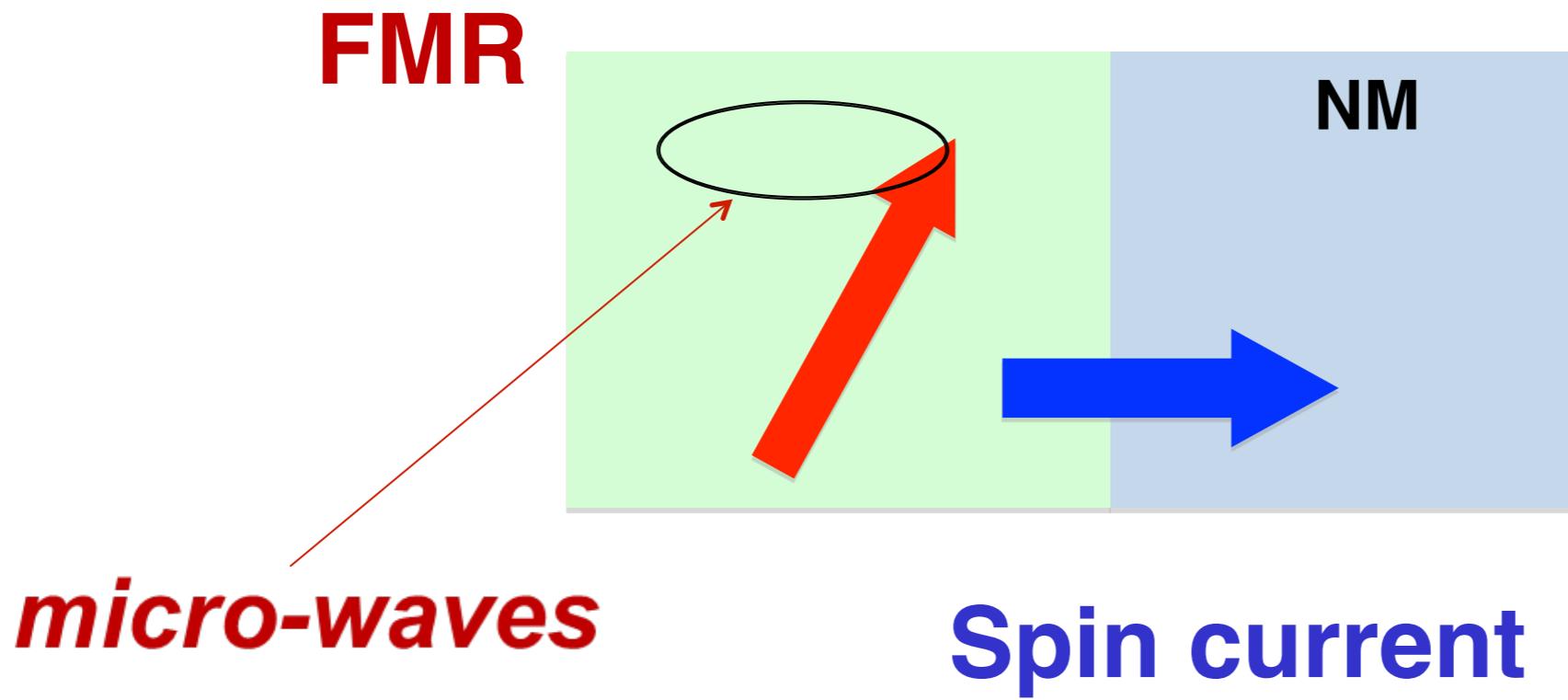
Pt/ $Y_3Fe_5O_{12}$ (YIG) junction

K. Uchida, H. Adahci, T. Kikkawa,
A. Kirihsara, M. Ishida, S. Yorozu,
S. Maekawa, and E. Saitoh,
“Thermoelectric generation based
on spin Seebeck effects”
(IEEE Proc., 104, 1946 (2016)).



Spin pumping

(spin current generation by FMR)

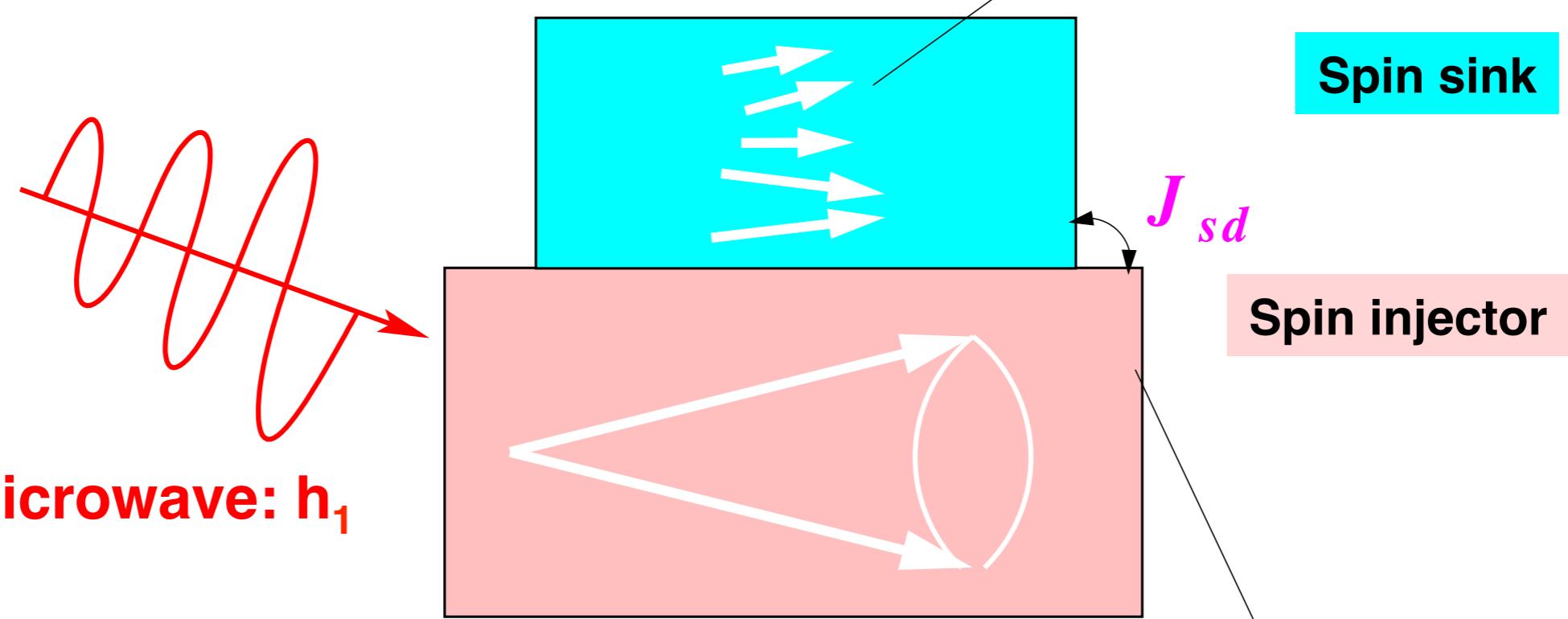


Spin current generation by FMR

Bloch eq. (s: spin accumulation)

$$\frac{d}{dt} s = \mathbf{J}_{sd} \mathbf{m} \times \mathbf{s} + (D_N \nabla^2 - \Gamma)(\mathbf{s} - s_0 \mathbf{m})$$

Nonmagnetic metal (SS)



Microwave: \mathbf{h}_1

Ferromagnet (SI)

$$\frac{d}{dt} \mathbf{m} = \mathbf{J}_{sd} \mathbf{s} \times \mathbf{m} + \gamma (\mathbf{H}_0 + \mathbf{h}_1) \times \mathbf{m} + \alpha \mathbf{m} \times \frac{d}{dt} \mathbf{m}$$

Landau-Lifshitz-Gilbert eq. (m: localized moment)

Linear response (busy slide, but important) !!

Bloch eq.: $\partial_t \mathbf{s} = J_{sd} \mathbf{m} \times \mathbf{s} + (D_N \nabla^2 - \Gamma)(\mathbf{s} - s_0 \mathbf{m})$ $(s_0 = \chi_N J_{sd})$

LLG eq.: $\partial_t \mathbf{m} = J_{sd} \mathbf{s} \times \mathbf{m} + \gamma (\mathbf{H}_0 + \mathbf{h}_1) \times \mathbf{m} + \alpha \mathbf{m} \times \partial_t \mathbf{m}$

1) Define the spin current injected into N by $J_s^{in} = (1/A_{contact}) \langle d\mathbf{s}^z/dt \rangle$.

From Bloch equation: $J_s^{in} \equiv \langle \partial_t S^z \rangle = \frac{J_{sd}}{A_{contact}} \text{Im} \int d\omega \langle s^+(\omega) m^-(-\omega) \rangle$

2) Linearize above two equations with respect to s^x, s^y, m^x, m^y .

$$s^+(\omega) = J_{sd} \chi_N(\omega) G_F(\omega) \gamma h_1^+(\omega)$$

$$m^-(\omega) = G_F(\omega) \gamma h_1^-(\omega)$$

$\chi_N(\omega)$: spin susceptibility of N

$G_F(\omega)$: spin susceptibility of F

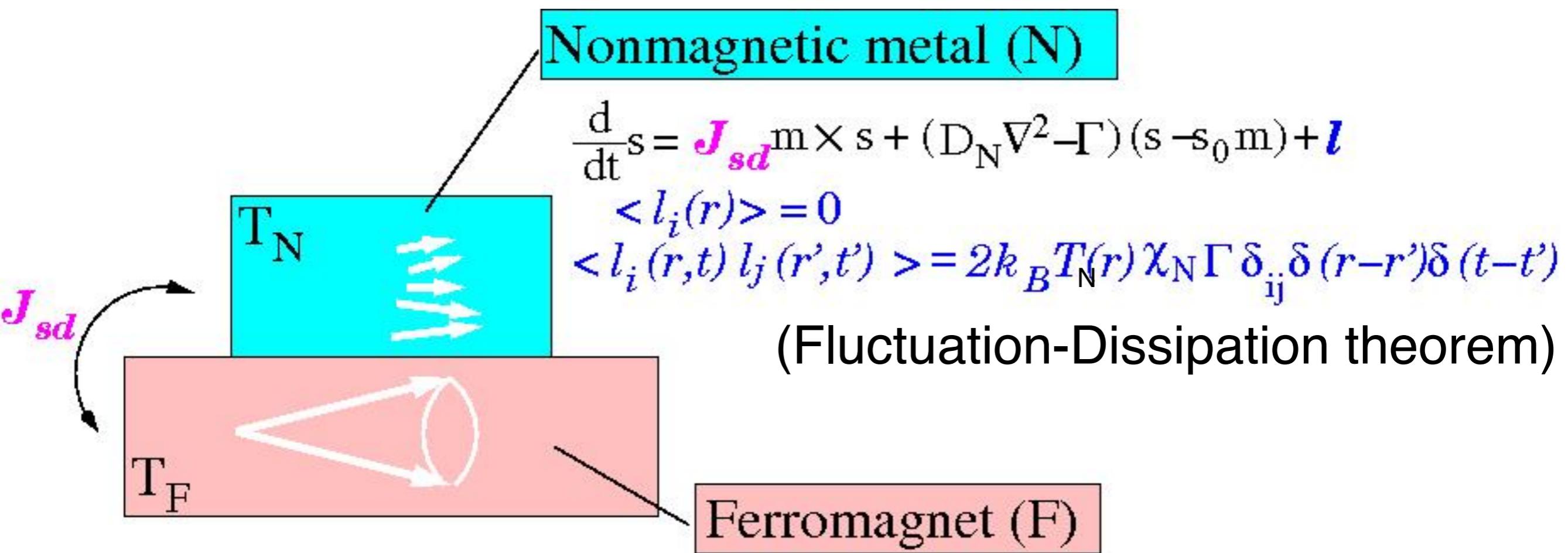
3) Substitute 2) into 1) and obtain the following result:

$$J_s^{in} = -\frac{J_{sd}^2}{A_{contact}} \int d\omega \text{Im} \chi_N(\omega) |G_F(\omega)|^2 \langle \gamma h_1^+(\omega) \gamma h_1^-(-\omega) \rangle$$

This is the general expression valid for any types of spin pumping!

Model for spin injection by thermal magnons

H. Adachi et al.: Phys.Rev. B83, 094410 (2011)).



$$\frac{d}{dt} \mathbf{m} = -\mathbf{J}_{sd} \mathbf{s} \times \mathbf{m} + \gamma (\mathbf{H}_{\text{eff}} + \mathbf{h}) \times \mathbf{m} + \alpha \mathbf{m} \times \frac{d}{dt} \mathbf{m}$$

$$\langle h_i(r) \rangle = 0$$

$$\langle h_i(r,t) h_j(r',t') \rangle = \frac{2k_B T_F(r) \alpha}{\gamma M_s} \delta_{ij} \delta(r-r') \delta(t-t')$$

(c.f., J. Xiao et al.: Phys. Rev. B81, 214418 (2010))

(Local) spin injection by thermal magnons

(H. Adachi et al.: Phys.Rev. B83, 094410 (2011))

Spin diffusion eq.: $\partial_t \mathbf{s} = J_{sd} \mathbf{m} \times \mathbf{s} + (D_N \nabla^2 - \Gamma)(\mathbf{s} - s_0 \mathbf{m}) + \mathbf{l}$ ($s_0 = \chi_N S_0 J_{sd}$)

LLG eq.: $\partial_t \mathbf{m} = J_{sd} \mathbf{s} \times \mathbf{m} + \gamma(\mathbf{H}_{eff} + \mathbf{h}) \times \mathbf{m} + \alpha \mathbf{m} \times \partial_t \mathbf{m}$

Injected spin current: $J_s^{in} \equiv <\partial_t s^z> = J_{sd} \text{Im} \int d\omega <s^+(\omega)m^-(-\omega)>$

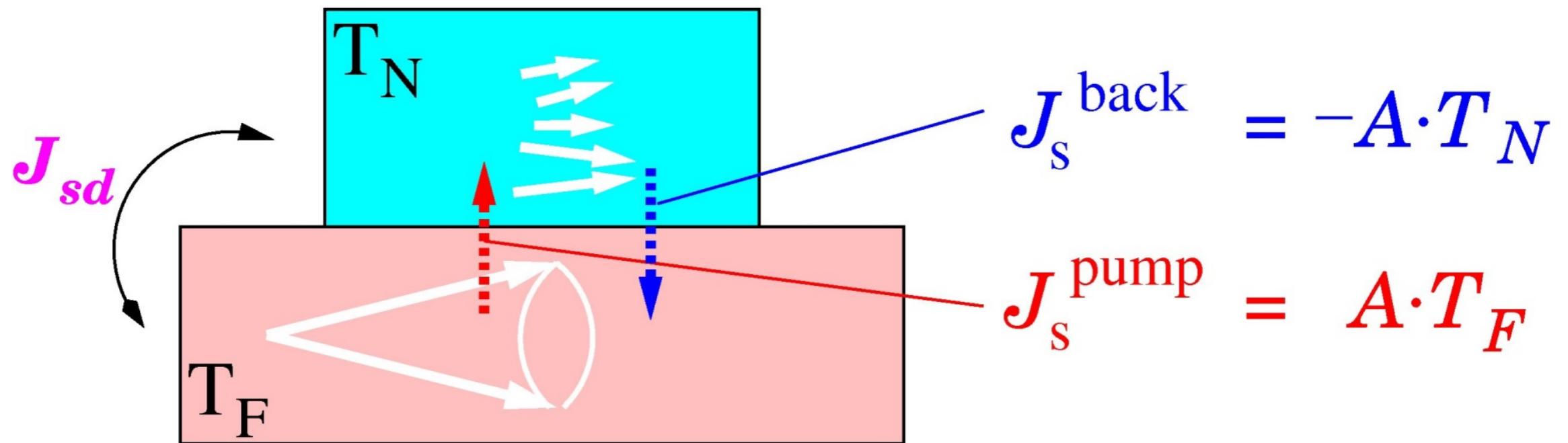
$$s^+(\omega) = \Gamma s_0 G_F^*(-\omega) \gamma h^+(\omega) + \chi_N^*(-\omega) l^+(\omega)$$

$$m^-(\omega) = G_F(\omega) \gamma h^-(\omega) + J_{sd} G_F(\omega) \chi_N(\omega) l^-(\omega) \quad (a^\pm \equiv a^x \pm i a^y)$$

$$J_s^{in} = J_{sd} \int d\omega \frac{1}{\omega} \text{Im} \chi_N(\omega) \text{Im} G_F(\omega) \left[\Gamma s_0 <\gamma h^+(\omega) \gamma h^-(-\omega)> - \alpha J_{sd} <l^+(\omega) l^-(-\omega)> \right]$$

$\uparrow \mathbf{J}_s^{\text{pump}}$ $\uparrow \mathbf{J}_s^{\text{back}}$

$$\therefore J_s^{in} = J_s^{pump} - J_s^{back}$$



Local non-equilibrium

$$\therefore J_s^{in} = A(T_F - T_N)$$

$$(A \propto J_{sd}^2 \int d\omega \frac{1}{\omega} \text{Im} \chi_N(\omega) \text{Im} G_F(\omega))$$

To get the non-equilibrium condition, we need heat flow!

Outline

Spin Seebeck Effect and Spin Peltier Effect:

i) Spin Seebeck Effect:

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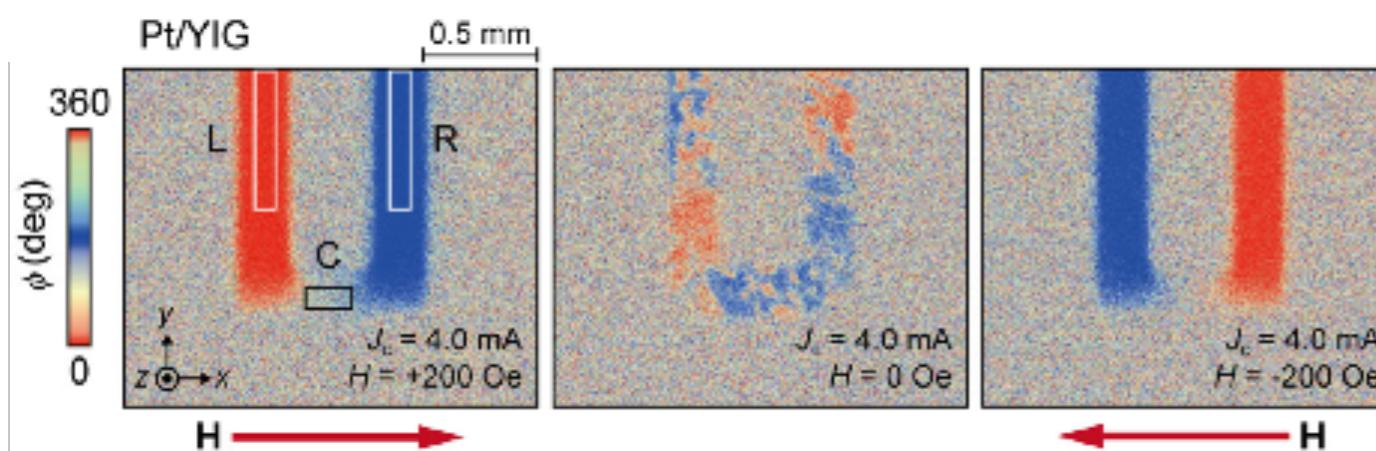
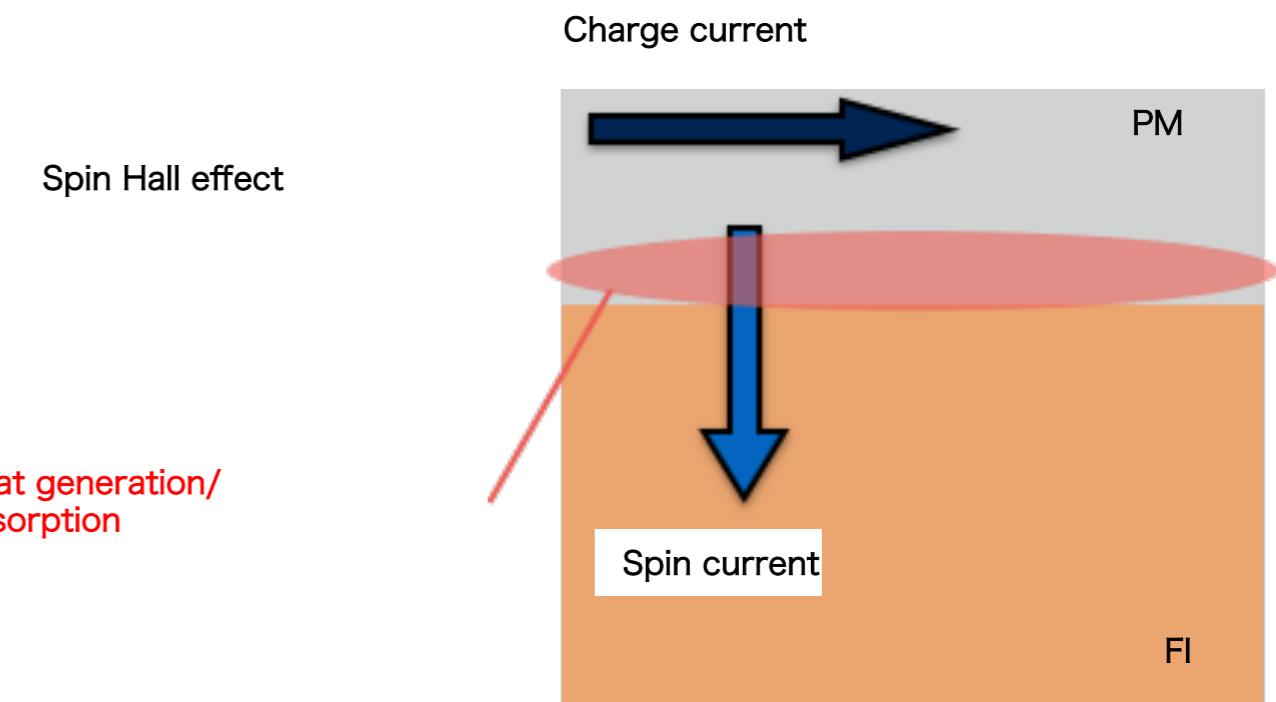
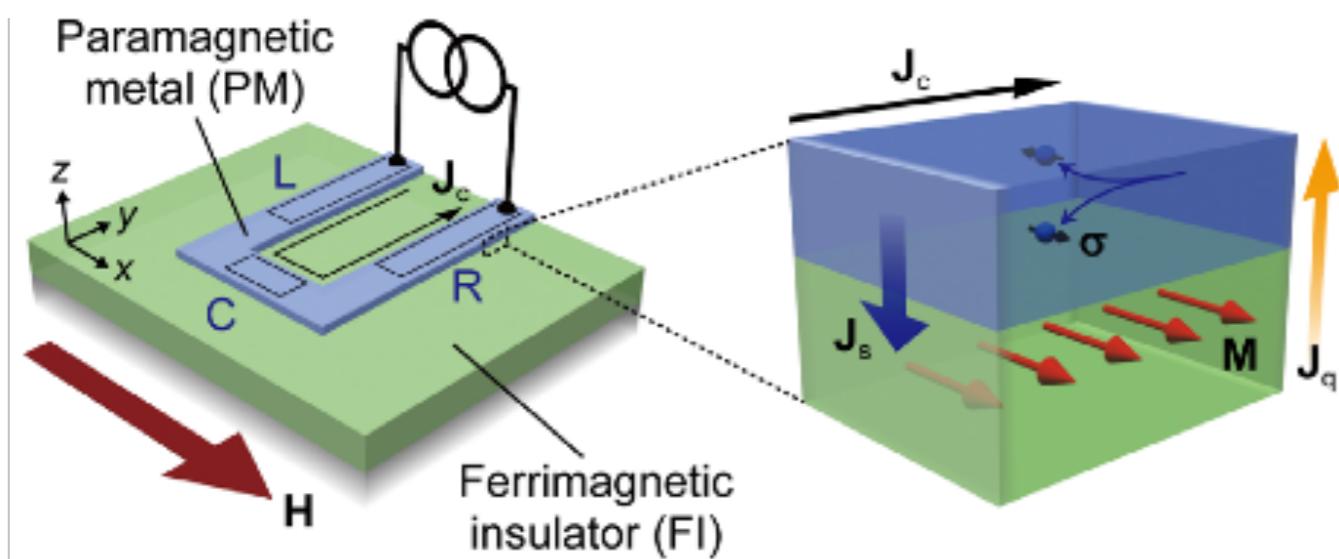
M. Matsuo (ASRC, JAEA).

Experiment:

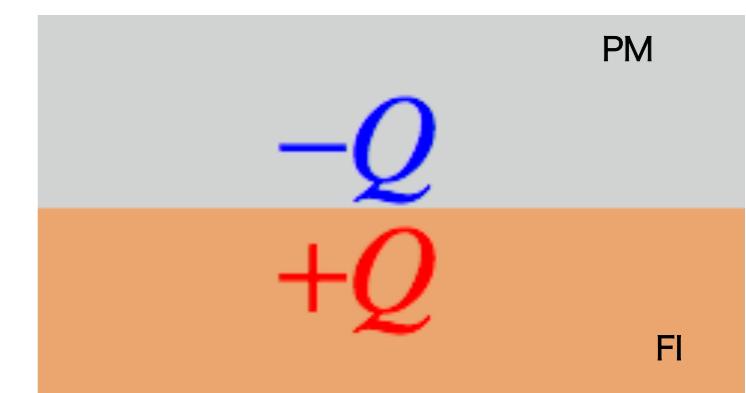
E. Saitoh (Tohoku U.) and members in his group,

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Spin Peltier Effect



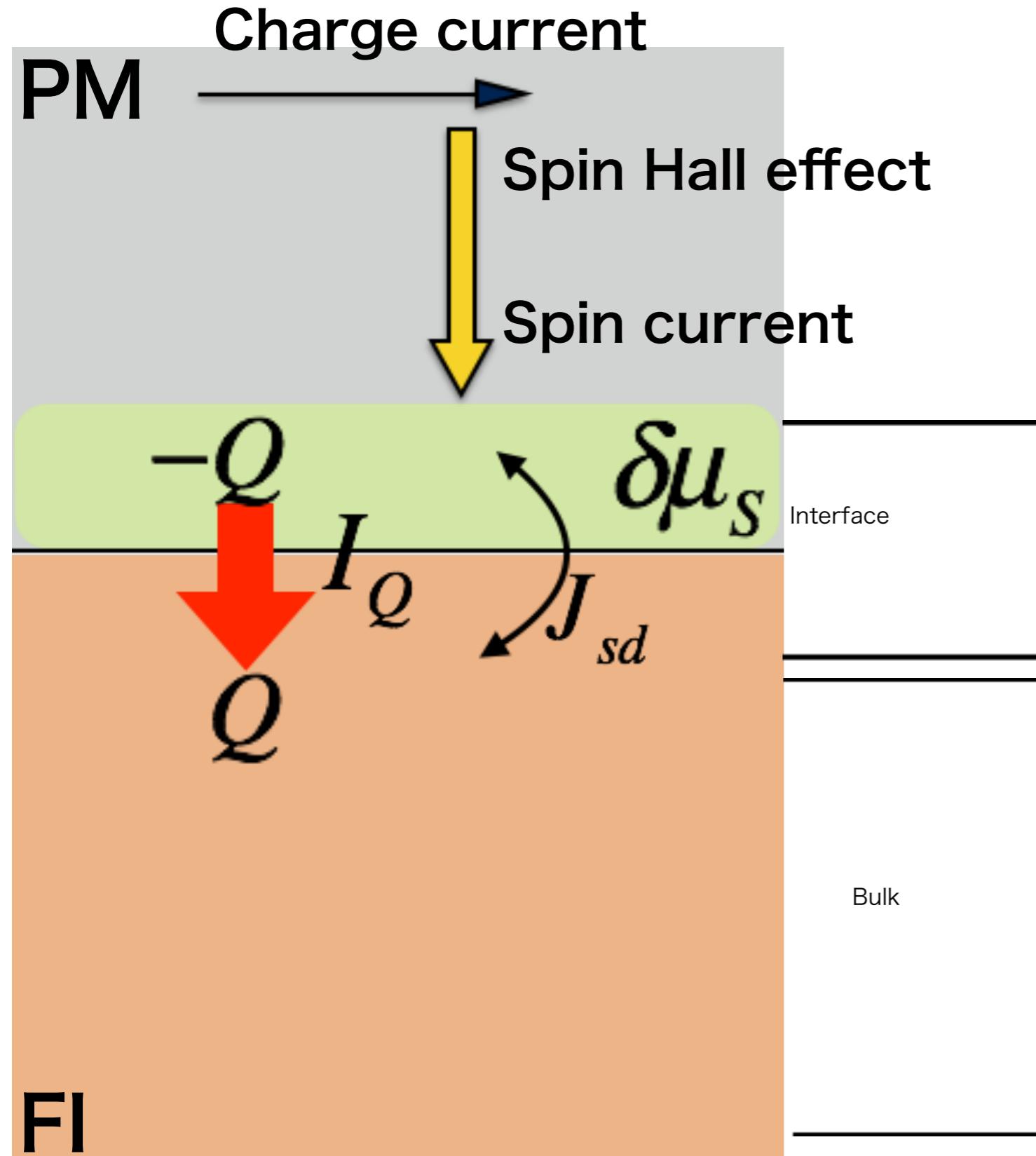
Daimon Nat. Common. (2016)
Flipse PRL (2014)



Daimon (2016)

Generation & absorption of heat driven by spin current

Theoretical model for spin Peltier effect



Spin accumulation
-> magnon current
-> heat current

Heat current

$$I_Q \propto \delta\mu_s$$

Temperature gradient

Kadanoff Baym equations
Of magnon and phonon

Spin current driven by spin accumulation

Spin accumulation at the interface (S. Zhang 2000)

$$\delta\mu_S = e\alpha_{SH} \lambda_{PM} \tanh(d_{PM} / \lambda_{PM}) E$$

Spin accumulation = Spin Hall angle \times Spin diffusion length \times Geometrical factor \times Electric field

Heat current injection into FI

$$I_Q = \langle \partial_t H_{FI} \rangle \dots \text{following Maki \& Griffin (1965)}$$

$$H^{\text{int}} = J_{sd} \sum_i \sigma_i^{PM} \cdot S_i^{FI}$$

$$I_Q = \delta\mu_S \times \Pi_{SPE}$$

Π_{SPE} : Spin Peltier coefficient

$$\Pi_{SPE} = \int_{kq\omega} \left[J_{sd}^2 \times \hbar\omega \times \text{Im } \chi_{q\omega}^{Pt} \times \text{Im } G_{k\omega}^{FI} \times \frac{\partial f}{\hbar\partial\omega} \right]$$

Exchange interaction \times Energy function in PM \times Spectral function in PM \times Spectral function in FI \times Distribution function

Spin & heat injection

Spin diffusion eq.: $\partial_t \mathbf{s} = (J_{sd} \mathbf{m} + \mathbf{b}) \times \mathbf{s} + (D_N \nabla^2 - \Gamma)(\mathbf{s} - s_0 \mathbf{m}) + \mathbf{l}$ $\mathbf{b} = \delta \mu_S \mathbf{z}$
 (s₀ = $\chi_N S_0 J_{sd}$)

LLG eq.: $\partial_t \mathbf{m} = J_{sd} \mathbf{s} \times \mathbf{m} + \gamma(\mathbf{H}_{eff} + \mathbf{h}) \times \mathbf{m} + \alpha \mathbf{m} \times \partial_t \mathbf{m}$

1) Define the spin and heat current injected into N.

From Bloch equation: $J_{Spin}^{in} \equiv \langle \partial_t s^z \rangle = J_{sd} \text{Im} \int d\omega \langle s^+(\omega) m^-(-\omega) \rangle$
 H. Adachi et al.: Phys. Rev. B 83, 094410 (2011).

From Heisenberg equation: $J_{Heat}^{in} \equiv \langle \partial_t H \rangle = J_{sd} \text{Im} \int d\omega \hbar \omega \langle s^+(\omega) m^-(-\omega) \rangle$

2) Linearize above two equations with respect to s and m.

$$s^+(\omega) = \Gamma s_0 G_F^*(\omega) \gamma h^+(\omega) + \chi_N^*(\omega + \delta \mu_S) l^+(\omega)$$

$$m^-(\omega) = G_F(\omega) \gamma h^-(\omega) + J_{sd} G_F(\omega) \chi_N(\omega + \delta \mu_S) l^-(\omega)$$

3) Substitute 2) into 1) and obtain the following results:

$$J_{Spin}^{in} = J_{sd} \int d\omega \text{Im} \chi_N(\omega + \delta \mu_S) \text{Im} G_F(\omega) \left[\Gamma s_0 \frac{\langle \gamma h^+(\omega) \gamma h^-(-\omega) \rangle}{\omega} - \alpha J_{sd} \frac{\langle l^+(\omega) l^-(-\omega) \rangle}{\omega + \delta \mu_S} \right]$$

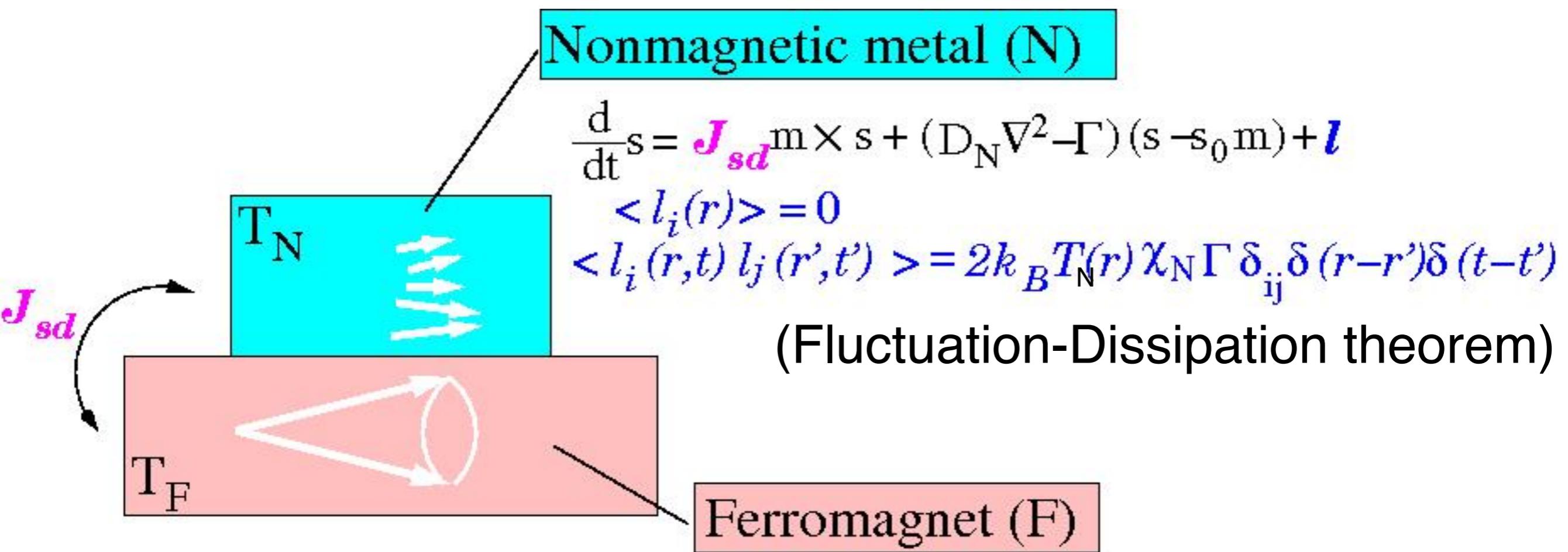
$\uparrow \mathbf{J}_S^{\text{pump}}$ $\uparrow \mathbf{J}_S^{\text{back}}$

$$J_{Heat}^{in} = J_{sd} \int d\omega \hbar \omega \text{Im} \chi_N(\omega + \delta \mu_S) \text{Im} G_F(\omega) \left[\Gamma s_0 \frac{\langle \gamma h^+(\omega) \gamma h^-(-\omega) \rangle}{\omega} - \alpha J_{sd} \frac{\langle l^+(\omega) l^-(-\omega) \rangle}{\omega + \delta \mu_S} \right]$$

$\uparrow \mathbf{J}_H^{\text{pump}}$ $\uparrow \mathbf{J}_H^{\text{back}}$

Model for spin injection by thermal magnons

H. Adachi et al.: Phys.Rev. B83, 094410 (2011)).



$$\frac{d}{dt} \mathbf{m} = -\mathbf{J}_{sd} \mathbf{s} \times \mathbf{m} + \gamma (\mathbf{H}_{\text{eff}} + \mathbf{h}) \times \mathbf{m} + \alpha \mathbf{m} \times \frac{d}{dt} \mathbf{m}$$

$$\langle h_i(r) \rangle = 0$$

$$\langle h_i(r,t) h_j(r',t') \rangle = \frac{2k_B T_F(r) \alpha}{\gamma M_s} \delta_{ij} \delta(r-r') \delta(t-t')$$

(c.f., J. Xiao et al.: Phys. Rev. B81, 214418 (2010))

Expression of spin & heat current

4) Substitute the correlation of noises into 3) :

$$J_{Spin}^{in} = J_{eff}^2 \int d\omega \operatorname{Im} \chi_N(\omega + \delta\mu_S) \operatorname{Im} G_F(\omega) \left(\frac{T_N + \Delta T}{\omega} - \frac{T_N}{\omega + \delta\mu_S} \right)$$

$$J_{Heat}^{in} = J_{eff}^2 \int d\omega \hbar\omega \operatorname{Im} \chi_N(\omega + \delta\mu_S) \operatorname{Im} G_F(\omega) \left(\frac{T_N + \Delta T}{\omega} - \frac{T_N}{\omega + \delta\mu_S} \right)$$

$$J_{eff}^2 := 2J_{sd}^2 \chi_N \alpha \Gamma k_B$$

$$\Delta T := T_F - T_N$$

5) Obtain the linear response theory as follows:

$$J_{Spin}^{in} = J_{eff}^2 \int_{-\infty}^{\infty} d\omega X(\omega) [\omega \Delta T + T_N \delta\mu_S]$$

$$J_{Heat}^{in} = J_{eff}^2 \int_{-\infty}^{\infty} d\omega \hbar\omega X(\omega) [\omega \Delta T + T_N \delta\mu_S]$$

$$X(\omega) := \frac{\operatorname{Im} \chi_N(\omega + \delta\mu_S)}{\omega + \delta\mu_S} \frac{\operatorname{Im} G_F(\omega)}{\omega} \sim \frac{\chi_N^2}{1 + (\omega/\Gamma)^2} \frac{1}{(\omega - \omega_0)^2 + (\alpha\omega)^2}$$

Spin Seebeck effect and spin Peltier effect

6) From the fluctuation dissipation theorem, 3) reduce as follows:

$$\begin{pmatrix} J_{Spin}^{in} \\ J_{Heat}^{in} \end{pmatrix} = \begin{pmatrix} L_{11} & L_{12} \\ L_{21} & L_{22} \end{pmatrix} \begin{pmatrix} \delta\mu_S \\ \Delta T / T \end{pmatrix}$$

$$L_{12} = 2J_{sd}^2 \alpha \Gamma k_B T_F \int d\omega \omega \frac{\text{Im } \chi_N(\omega + \delta\mu_S)}{\omega + \delta\mu_S} \frac{\text{Im } G_F(\omega)}{\omega}$$

$$= L_{21}$$

Onsager's reciprocal relation

“Kelvin relation” for interconversion of heat and spin currents

$$J_{Spin}^{in} = S_{SSE} \Delta T$$

$$J_{Heat}^{in} = \Pi_{SPE} \delta\mu_S$$

$$\Pi_{SPE} = TS_{SSE}$$

Generation of heat by spin current

$$Q^{FI} = \int_{k\omega} \hbar\omega \delta G_{k\omega}^{<,FI}$$

Heat = $\frac{\text{Energy of magnon}}{\text{magnon}} \times \frac{\text{Number density of magnons}}$

$$\delta G_{k\omega}^{<,FI}$$

$$= \text{Im } G_{k\omega}^{R,FI} \times \delta f_{k\omega}^{(2),FI}$$

Spectral function

Distribution function



Rate equation of magnons

$$\int_{k\omega} \frac{\hbar\omega \delta G_{k\omega}^{<,FI}}{\tau_{mag}} = I_Q$$

$$\tau_{mag} = \frac{1}{\alpha\omega}$$

α : Gilbert damping constant

$$Q^{FI} = \langle \tau_{mag} \times I_Q \rangle_{k\omega} \propto \delta\mu_S$$

$$\langle \tau_{mag} I_Q \rangle_{k\omega} := \int_{k\omega} \tau_{mag} I_Q(k, \omega)$$

Heat = $\frac{\text{Relaxation time}}{\text{time}} \times \text{Heat current}$

$$I_Q = \int_{k\omega} I_Q(k, \omega)$$

$$= J_{sd}^2 \int_{k\omega} \omega \text{Im} \chi_{q\omega}^{R,Pt} \text{Im} G_{k\omega}^{R,FI} \frac{\partial f}{\partial \omega}$$

Estimation of temperature change

Pt/YIG system

$$Q^{YIG} = \delta\mu_s^{Pt} \times N_{int} \left[\frac{\delta\alpha}{\alpha} \left(\frac{k_B T}{\hbar\omega_M} \right)^{3/2} \gamma_{SPE/SP} \right] \delta\mu_s^{Pt} = 2.3 \times 10^{-7} [eV] \text{ Daimon 2016}$$

$$N_{int} = 1 \times 10^{11}$$

$$\delta\alpha = 3.6 \times 10^{-3}$$

$$\alpha = 10^{-5}$$

$$\frac{k_B T}{\hbar\omega_M} = 0.53 \quad @300K$$

$$\gamma_{SPE/SP} = \frac{\int_0^1 dy \int_{x_0}^{x_M} dx \frac{\sqrt{y}}{(1+y)^2 + (xk_B T \tau_{sf}/\hbar)^2} \frac{x\sqrt{x-x_0}}{4 \sinh^2(x/2)}}{\int_0^1 dy \frac{\sqrt{y}}{(1+y)^2 + (\omega_0 \tau_{sf})^2}} \sim 1$$

$$x_0 = \frac{\hbar\gamma H_0}{k_B T}, \quad x_M = \frac{\hbar\omega_M}{k_B T}$$

Estimation of ΔT

$$\Delta T = \frac{Q^{YIG}}{C_v^{YIG}} \sim 20mK$$

(cf: 0.5mK [Daimon 2016])

$$C_v^{YIG} = 5.5 \times 10^{-10} [J/K]$$

Onsager's relation

Spin current

$$I_S := \langle \partial_t \sigma^z \rangle$$

Heat current

$$I_Q = \langle \partial_t H_{FI} \rangle$$

Transport coefficients

$$\begin{pmatrix} I_S \\ I_Q \end{pmatrix} = \begin{pmatrix} L_{11} & L_{12} \\ L_{21} & L_{22} \end{pmatrix} \begin{pmatrix} \delta\mu_S \\ -\Delta T / T \end{pmatrix}$$

Spin Seebeck coefficient

$$S_{SSE} := L_{12} / T \quad L_{12} = \int_{kq\omega} \left[J_{sd}^2 \operatorname{Im} \chi_{q\omega}^{PM} \operatorname{Im} G_{k\omega}^{FI} \left(-T \frac{\partial f}{\partial T} \right) \right]$$

Spin Peltier coefficient

$$\Pi_{SPE} := L_{21} \quad L_{21} = \int_{kq\omega} \left[J_{sd}^2 \omega \operatorname{Im} \chi_{q\omega}^{PM} \operatorname{Im} G_{k\omega}^{FI} \frac{\partial f}{\partial \omega} \right] = L_{21}$$

Onsager's relation

Kelvin relation for spin and heat current in PM/FM

$$\frac{\partial f}{\partial \omega} = -\frac{T}{\omega} \frac{\partial f}{\partial T}$$

$$\Pi_{SPE} = TS_{SSE}$$

In conclusion:

Heat vs. Electricity

	To get Electricity	To get Heat
Charge	Seebeck effect	Peltier effect
Spin	Spin Seebeck effect Uchida 2008	Spin Peltier effect Flipse 2014 Daimon 2016